Part I: Prove that \( p(n) \leq \frac{p(n-1) + p(n+1)}{2} \), for \( n \in \mathbb{N} \).

HINT: It can be shown that this is equivalent to \( p(n+1) - p(n) \geq p(n) - p(n-1) \).