For any group G, we define $Z(G) = \{x \in G : \forall y \in G, xy = yx\}$, the set of elements in G that commute with everything in G. Prove that $Z(G)$ is a subgroup of G.