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## Math 254 Spring 2014 Exam 4

Please read the following directions:

Please print your name in the space provided, using large letters, as “First LAST”. Books, notes, calculators, and other aids are not permitted on this exam. Please write legibly, with plenty of white space. Please put your answers in the designated areas. Show all necessary work in your solutions; if you are unsure, show it. Cross out work you do not wish graded; incorrect work can lower your grade. All problems are worth 5-10 points; your total will be scaled to the standard 100 point scale. You have approximately 30 minutes.

Extra credit may be earned by handing in revised work in class on Friday 3/7; for details see the syllabus. You will find this exam on the instructor’s webpage later today.

1. Carefully state the definition of “span”. Give two (different) sets of vectors from  $M_{2,2}$ , neither of which may have the vector  $I$  in their span.

2. Carefully state five of the eight vector space axioms.

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3. Prove that for any vector space  $V$ , and for any vector  $\bar{v} \in V$ , that  $0\bar{v} = \bar{0}$ .

4. Let  $V \subseteq P_2(t)$  be defined by  $V = \{p(t) : \forall t, p(t) \geq p'(t)\}$ , where  $p'(t)$  denotes the derivative. Determine whether or not  $V$  is a vector space.

5. Set  $V = P_2(t)$ . Give any two subspaces  $U_1, U_2$  such that  $U_1 \oplus U_2 = V$ . Be sure to justify.